

## 2/4 B.Tech - THIRD SEMESTER

EC3T2

Probability Theory and Stochastic Process

Credits: 3

Lecture: 3 periods/week

Internal assessment: 30 marks

Tutorial: 1 period /week

Semester end examination: 70 marks

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**Prerequisite:** Engineering Mathematics-I (EC1T1), Engineering Mathematics-II (EC 2T1)

### Course Objectives:

- To acquire the fundamental knowledge in probability concepts
- To manage situations involving more than one random variable and functions of random variables in engineering applications.
- To understand the principles of random signals and random processes
- To be acquainted with systems involving random signals and to analyze the response of random inputs to linear time invariant systems

### Learning Outcomes:

After successful completion of the course, Graduates shall be able to

- Define probability and interpret probability by modeling sample spaces.
- Construct the probability distribution of a random variable, based on a real-world situation, and use it to compute expectation and variance
- Solve the problems involving multiple random variables.
- Apply the concepts of random process in communication and signal processing
- Evaluate response of a linear system to Random Process.

### UNIT- I

**Probability:** Probability introduced through Sets and Relative Frequency, Experiments and Sample Spaces, Types, Events, Probability Definitions and Axioms, Mathematical Model of Experiments, Probability as a Relative Frequency, Joint Probability, Conditional Probability, Total Probability, Baye's Theorem, Independent Events, Bernouli Trails.

### UNIT- II

**The Random Variable:** Definition of a Random Variable- Types, Conditions, Distribution and Density functions, Properties, Types, Examples, Conditional Distribution and Density, Properties.

**Operations on One Random Variable:** Expectation, Moments, Chebychev's Inequality, Marcov's Inequality, Characteristic Function, Moment Generating Function, Transformations of a Random Variable

### UNIT- III

**Multiple Random Variables:** Vector Random Variables, Joint Distribution Function, Properties, Conditional Distribution and Density, Statistical Independence, Sum of Random Variables, Central Limit Theorem.

**Operations on Multiple Random Variables:** Expected Value of a Function of Random Variables, Joint Moments, Joint Characteristic Functions, Jointly Gaussian Random Variables, Properties, Transformations of Multiple Random Variables, Linear Transformations of Gaussian Random Variables

#### **UNIT- IV**

**Random Processes –Temporal Characteristics:** The Random Process Concept, Classification, Distribution and Density Functions, Stationarity and Independence, Time Averages and Ergodicity, Correlation Functions and their Properties, Covariance Functions, Gaussian Random Process, Poisson Random Process.

**Spectral Characteristics:** The Power Spectrum: Properties, The Cross-Power Density Spectrum, Properties, Relationship between Power Spectrum and Correlation Functions.

#### **UNIT- V**

**Linear Systems with Random Inputs:** Random Signal Response of Linear Systems, Spectral Characteristics of System Response, Band pass, Band-Limited and Narrowband Processes, Properties, Modeling of Noise Sources

### **Learning Resources**

#### **Text Books:**

1. Probability, Random Variables & Random Signal Principles - Peyton Z. Peebles, TMH, 4<sup>th</sup> Edition, 2001.

#### **References:**

1. Probability, Random Variables and Stochastic Processes – A. Papoulis and S. Unnikrishna Pillai, PHI, 4<sup>th</sup> ed., 2002.
2. Statistical Theory of Communication - S.P. Eugene Xavier, New Age Publications, 2003.
3. Probability Methods of Signal and System Analysis. George R. Cooper, Clive D. MC Gillem, Oxford, 3<sup>rd</sup> ed., 1999
4. Signals, Systems & Communications - B.P. Lathi, B.S. Publications, 2003.
5. Communication Systems Analog & Digital – R.P. Singh and S.D. Sapre, TMH, 1995.